











# Gibbs' Phenomena



Theorem: If a series of continuous function converges uniformly in a closed interval then the limit function is continuous.

- Story- Michelson noticed an overshoot when going from coefficients of a Fourier Series back to a function. When he asked local mathematicians about the problem, they said it was his computer.
- Gibbs, from Yale, listened and looked into the matter.

### Gibbs' Phenomena



Simplest direct approach is to expand a standard discontinuity into a Fourier Series of a finite number of terms.

After rearranging, then find the location of the first maximum and finally the corresponding height of the functions there.

Many people had the opportunity to discover the Gibb's phenomena, and it was Gibbs that made the effort.

## **Hamming Assertion**



There are opportunities all around and few people reach for them.

Pasteur said, "Luck favors the prepared mind."

This time the person who was prepared to listen and help a first class scientist in his troubles (Gibbs) got the fame.

# Cauchy's Textbooks



### Contradictions

- A convergent series of continuous functions converge to a continuous function.
- The Fourier expansion of a discontinuous function.

The concept of uniform convergence. The overshoot of the Gibb's phenomena occurs for any series of continuous functions, not just Fourier Series.

# Gibb's Phenomena Patrici Scie S. S. Sa Pa Recroscolad Plass Figure 15-2

# Another Feature of a Fourier Series



If the function exists then the coefficients fall off like 1/n.

If the function is continuous and the derivative exists then the coefficients fall off like 1/n<sup>2</sup>.

If the first derivative is continuous and the second derivative exists then they fall off like 1/n<sup>3</sup>, etc.













